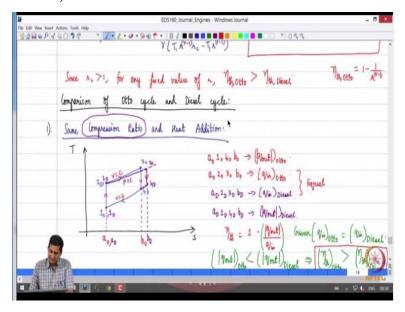
Fundamentals of Automotive Systems Prof. C.S. Shankar Ram Department of Engineering Design Indian Institute of Technology-Madras

Lecture-11 Dual Cycle and Engine performance Part 01

(Refer Slide Time: 00:15)

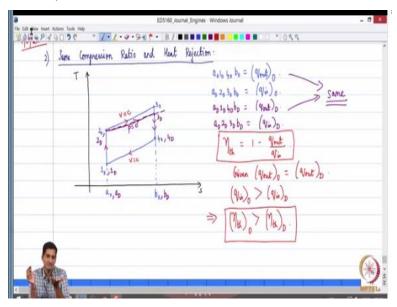


Ok, greetings, so welcome to today's class, so, just a quick recap of what we did yesterday. So in yesterday's class we considered the air standard otto cycle and air standard diesel cycle. We looked at the processes of those 2 cycles and we identified that the main difference between them was that of the heat addition process right. In the otto cycle heat addition was assumed to take place or almost constant volume.

In the diesel cycle, heat addition was assumed to take place at almost constant pressure, there is a main difference and we went and did some analysis using a conservation of energy and use the process relationships for isentropic process and ideal gas equation of state to get expressions for the thermal efficiency of the 2 cycles. So and we just started off at one case where we wanted to compare the otto cycle and the diesel cycle.

So as we realized from the analysis, if you fix the same value of compression ratio r the air standard otto cycle has a higher thermal efficiency than that of the diesel cycle we just wanted to essentially investigated further. So we considered one case where we had the same compression ratio and heat addition, today I am just going to do one more example and then like we will move on to what is called as a dual cycle ok.

(Refer Slide Time: 01:50)



So let me do a second case where we still consider the same compression ratio for both the otto and the diesel cycle. But now let us consider the same amount of heat being rejected ok, so that is the scenario that we are going to consider now. So let me once again quickly draw the Ts diagram for the otto cycle and then we will look at what happens in terms of the diesel cycles.

So let me call this 10 this is 20 and we have constant volume heat addition, go to 30 and then isentropic expansion come to 40 and then constant volume heat rejection ok. So we need to carefully mark all the processes when we draw these diagrams ok, so this is the Ts diagram. Now as we have already discussed the area a 0, 1, 4 o b o is equal to the heat rejected in the otto cycle and the area a 0 2 o 3 o b o is a heat input given to the otto cycle right.

So that is something which we have already learned, now once again let us start from the same initial state ok. So 1 D is a same as 10 then what we do is that like, we have isentropic compression. So where should 2 D b same as 2 o why, because same compression ratio. So as we

realized from the analysis T 2 as T 1 times r power gamma - 1. So T 1 is the same for both cycles, r is the same that is the condition we are given.

So T 2 should be the same, so 2 D should coincide with 20, so now let us draw the constant pressure line passing to 2 D and that is going to be something like this right. So that is the constant pressure line right passing through 2 D, so we are given that the heat rejected is now the same ok. So that means a D the area a D, of course a D is the same as a 0 now ok, a D 1 D 4 D b D should be equal to a 0 1 o 4 o b o ok, so these 2 should be is the same.

So what does that tell us, because even in the diesel cycle, heat rejection is done at constant volume right ok. So a o 1 o and 1 D coincide a o and a D coincide, so what can we say about 4 D it should be the same as 40 right. Otherwise there is no way the area a D 1 D 4 D b D will be the same as a o 1 o 4 o b o because in both the otto cycle and the diesel cycle heat rejection takes place at constant volume and there is only one constant volume line passing through 1o and 1 D.

So the point 4 D must coincide with 4o, so then the state b D will be the same as b o right. So we have identified 4 D now how do I identify 3 D, please remember 3 D, 4 D is isentropic expansion. So 3 D must lie on the vertical line passing through 4 D in the Ts diagram. So and then 3 D should also lie on the constant pressure line passing through 2 D. So the intersection of the constant pressure line passing through 2 D and the constant entropy line passing through 4 D should be 3 D and what is that point it is here right.

So as a result this is my diesel cycle correct, so we have identifying this one, so please note the area a D 2 D 3 D b D is the heat input given in the diesel cycle. Now we know that the thermal efficiency is going to be equal to 1 - q out by q in ok, we are given that q out in the otto cycle and q out in the diesel cycle or pretty much the same that is like I reject the same amount of heat energy ok in both the cycles, now what can you say about q in.

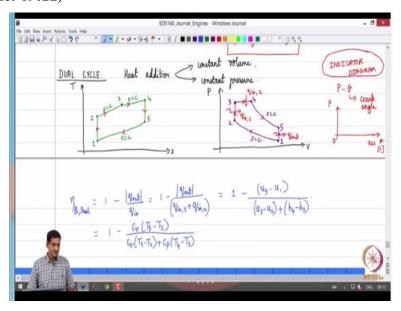
So please note q in the otto cycle is a o 2 o 3 o b o right, q in the diesel cycle as a D 2 D 3 D b D which is bigger otto cycle right. So then what can you say about the thermal efficiencies, please note that the expression for thermal efficiency is this. So the second term that appears a thermal

efficiency q out which is the numerator is the same for both cycles, q in which as a denominator is larger for otto so the ratio is smaller for otto cycle right.

So we are subtracting a smaller number from 1 in the otto cycle, so which efficiency will be greater otto right. So the otto cycle will have more thermal efficiency than the diesel cycle as long as the compression ratio is the same right, so that is the main takeaway ok. But as we will discuss when we look at the actual combustion process, the phenomena of knocking typically restricts the maximum compression ratio in petrol engines or gasoline engines right.

So we are not going to have the same compression ratio in gasoline or spark ignition engines when we compare it, compare them in diesel engines right. So as a result, we will see that the compression ratios would not be the same, however if the compression ratios were the same, you see that the otto cycle is more efficient than the diesel cycle ok. We will discuss this point as we go now right as we go to actual engine performance and do the analysis, we will discuss it further ok.

(Refer Slide Time: 09:11)



So the next air standard cycle that we will discuss is what is called as a dual cycle. So in the last class when we motivated the otto cycle and the diesel cycle you know the constant volume heat addition process and constant pressure heat addition process are typically motivated by looking at the actual engine curve right. In reality you know like if you look at the actual engine data,

you know we are not going to see the combustion process happening at almost constant volume or almost constant pressure ok, it is going to be a mix of both.

So the question is if the otto cycle and the diesel cycle do not approximate the actual cycle well enough, what does an alternative to do first (()) (10:00) analysis. So that answer is the dual cycle, so in the dual cycle, what we do is that, we consider that the heat addition process takes place in 2 phases, the first one is it constant volume, the second one is in a constant pressure, of course we are making all these approximations.

So that we can derive analytical expressions which are simple enough to what to say do a pen and paper analysis. So that is the motivation, so in a dual cycle, we consider that the heat addition process takes place in 2 phases. So if I were to draw the Ts diagram for the dual cycle, it will looks something like this. So I will start with state 1 what will happen is that like I will go to state 2 the compression processes going to be isentropic.

Then there will be 2 heat addition processes one at constant volume another at constant pressure. So first I will have a constant volume heat addition process then I have a constant pressure heat addition process then we will have isentropic expansion then the heat rejection process will is reasonable enough to be assumed at constant volume once again ok. So this is the dual cycle, so you can see that the heat addition process now consists of 2 sub processes ok constant volume process and a constant pressure process.

So if I were to draw the PV diagram for the same process, so and then I draw it here. So 1 to 2 will be isentropic compression, 2 to 3 will be constant volume heat addition, 3 to 4 will be constant pressure heat addition, 4 to 1 is isentropic expansion sorry 4 to 5, and 5 to 1 will be will be constant volume heat rejection. So the processes these were take place like this ok, so consequently there are 2 heat addition process that scholars q in 1 and q in 2 and this is the heat rejection process q in right, so that is the PV diagram of the dual cycle.

So I hope it is clear why the term dual came into being right, so the heat addition process has to stay this first at constant volume then at constant pressure. So the idea is the whether the dual

cycle can better approximate the actual engine cycle ok. So in this analysis we are using the PV diagram just a quick aside, you know like in engine analysis you will also encountered the P - theta diagram ok P - theta diagram theta being the crank angle or the crank shaft angle ok.

So as we know in a 4 stroke engine, 1 operating cycle is completed and 2 revolutions of the crankshaft. So this is 1 cycle, so how many degrees will constitute 1 cycle and a P - theta diagram, suppose if we were to plot a P-theta diagram I start from 0 degrees right 1 cycle will go to 720 ok. So it will be spread out, so you would not see a loop like this ok because then you need to mark BDC, TDC repeatedly ok.

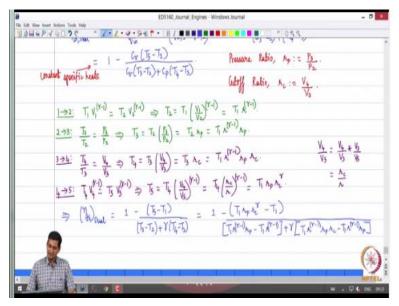
Here we mark at 1 volume and then we understand how what is happening, so there it will be spread out ok. So P - theta diagram is also used by use for some analysis ok like in engine and you can obviously see that there is a 1 to 1 correlation between V and theta ok once you fix an origin, starting point, you can always figure out, you can always correlate V and theta right. So these diagrams are what are called as indicator diagrams ok, the term indicator diagrams is use to represent these diagrams ok fine.

So that is a quick aisle right, so now let us come back to our analysis right of the dual cycle. So once again the thermal efficiency of the dual cycle is as we know from first of thermodynamics, what we derive is going to be 1- q out by q in. However now q in will consider will consists of 2 parts q in 1 + q in 2 ok, so those will be the 2 parts. Now from yesterday's from the last classes analysis you know like we know how to write the expressions for q out right.

So let me put the magnitude to be consistent, so we are going to be look at the magnitude of q out ok. So we already know how to do this analysis right, so let me directly write the expressions. So what do you think will be q out now, it will be u5 - u1 correct, so what will be q in 1, it will be u3 - u 2 because the constant volume heat addition process is from 2 to 3. Then what about 3 to 4, it will be now h4 - h3 right because it is a constant pressure heat addition process ok.

So considering constant specific heats, we are going to get C v times T 5 - T 1 divided by C v times T 3 - T 2 + C p times T 4 - T 3 ok, so that is the simplified expression ok.

(Refer Slide Time: 16:52)



So here we are considering constant specific heats alright, so now the question that arises is the following right. So how do we then simplify right we have all temperatures, by now we are familiar the process right we have to use the process relationships, let us go from one process at a time and then like we eliminate the temperatures right. So but before doing that, you know like quick definitions that 2 parameters you know like the first one is what is called as a pressure ratio r P which is defined as P 3 by P 2.

So in the constant volume heat addition process the volume is constant but the pressure is increasing right. So the pressure ratio r subscript P tells me what is the ratio of P3 and P2 ok that we encountered in the constant volume heat addition process and we have already encountered the cut off ratio alright, cut off ratio r subscript C is going to be now V 4 by V 3. Because that is the 3 to 4 is the constant pressure heat addition process right.

So that is the cutoff ratio, now let us look at each process at a time. So now if you look at 1 to 2, what is 1 to 2, it is isentropic compression, so what is the process relationship will have T 1 V 1 power gamma - 1 will be equal to T 2 V 2 power gamma - 1. So that essentially results in T 2 being T 1 V 1 by V 2 to the power gamma - 1 right and what is V 1 by V 2, r, so this is a

standard relationship by now we are familiar with this right, so T 2 is going to be T 1 times r power gamma - 1.

So then we consider the constant volume heat addition process 2 to 3, so we know that since the volume is constant the ratio of temperature is going to be equal to the ratio of pressures, how do we get that from the ideal gas equation of state right. So this is the process relationship for this constant volume heat addition process. So this will give me T 3 equals T 2 times P 3 by P 2 what is P 3 by P 2 r P and then I substitute for T 2 I am going to get T 1 r power gamma - 1 times r P right.

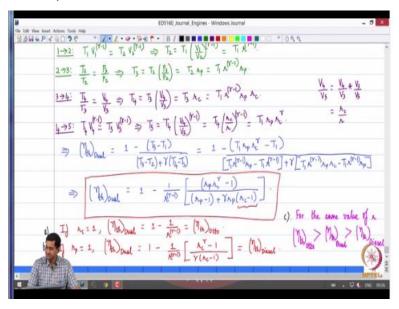
So that is the second process then let us look at the constant pressure heat addition process, so what is going to be the process relationship for constant pressure heat addition process T4 by T3 is going to be equal to V4 by V3. So this implies T 4 = T 3 V 4 by V 3 and V 4 by V 3 is r C, then I substitute for T 3 we will get T 1 r power gamma - 1 r P r C right, that is T 4. Then we consider process 4 to 5, which is isentropic expansion that is going to be the T 4 V 4 power gamma - 1 that is going to be equal to T 5 V 5 power gamma - 1.

So this will give me T 5 = T 4 V 4 by V 5 gamma - 1 and what is V 4 by V 5, I can rewrite it as V 4 by V 3 times V 3 by V 5, what is V 4 by V 3 is the r C, what is V 3 by V 5 it is going to be 1 by r V 5 by V 3 is r, V 3 by V 5 is going to be the reciprocal r right, so I will have r C by r. So this will be r C by r to the power gamma - 1, if I substitute for T 4 what I am going to get r power gamma - 1 will cancel off, I will get r P r C to the power gamma that is what I will get for T 5 right.

Now we are all set, so we go back and then look at the thermal efficiency of the dual cycle. So that is going to be 1 - T 5 - T 1 divided by T 3 - T 2 + gamma times T 4 - T 3, so what have I done I have just divided by C v right and C p by C v is going to be the ratio of specific heats correct. So now we go and substitute all the temperatures, so what will happen T 5 is going to be equal to T 1 r P r C power gamma - T 1.

And in the denominator, T 3 is going to be T 1 r power gamma - 1 r P, T 2 is T 1 r power gamma-1 there is a first term then plus gamma times T 4 is T 1 r power gamma-1 r P r C - T 3 right T 3 is what, T 1 r power gamma - 1 r P am I correct. So I am substituting the appropriate values of the temperatures that we have already derived.

(Refer Slide Time: 23:42)



So if we simplify we can immediately see that this t1 can be cancelled in the numerator and denominator right in the second term. So what we are going to have is the following, so you can pull out r power gamma - 1 common from the denominator then we are going to have the numerator r P r C power gamma - 1 divided by r P - 1 + gamma r P r C - 1 ok. So this is what we have, so this is the expression for the thermal efficiency of the air standard dual cycle ok.

You can immediately observe that it depends on the compression ratio r the pressure ratio r P the cutoff ratio r C and gamma right. So those are the 4 parameters that affect the thermal efficiency of the dual cycle ok. Now we can immediately observe from this expression that if r = 1, what happens to the thermal efficiency expression. If r C is 1 what happens the above expression reduces to 1 - 1 by r power gamma - 1 which is nothing but the otto right.

If r C is 1, you see that the second term vanishes, this term vanishes and the denominator becomes r P - 1 cancel, we are going to get 1 - 1 by r power gamma - 1 am I correct. So that is the thermal efficiency of the air standard otto cycle, so if r C is 1 that means that you know like,

what does it mean, there is no constant pressure heat addition right, the states 3 and 4 coincide alright, so that is a meaning.

So if r P is 1, what do you expect, of course now there is no constant volume heat addition process. So if you substitute r P = 1, this is going to become 1 - 1 divided by r power gamma - 1 multiplied by r C power gamma - 1 divided by gamma times r C - 1. And what is this expression, if we go to the analysis of diesel cycle that we did, that is the thermal efficiency of the air standard diesel cycle correct.

So you can see that the dual cycle boils down to the diesel cycle ok and in general for the same value of r ok compression ratio. We already learned that the thermal efficiency of the otto cycle is going to be greater than the thermal efficiency of the diesel cycle and the thermal efficiency of the dual cycle is going to be somewhere in between ok, so this can be shown right. So essentially the value of thermal efficiency of the otto cycle with the highest followed by the diesel cycle followed by the diesel cycle for the same value of compression ratio ok.

So these are 3 let us say we call 3 observations ok, so let me call them as a, b and c ok, so some points to note ok. So that completes a simple analysis of what are called air standard cycles, we learned the otto cycle, the diesel cycle and the dual cycle. And the main advantage of these cycles is that like, despite the assumptions that we make, it can be used to get a first cut idea about the particular engines performance right using some approximations you know like, so that is the main idea.